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EXPERIMENTAL DETERMINATION OF PITCHING MOMENT AND DAMPING COEFFICIENTS

OF A CONE IN LOW DENSITY, HYPERSONIC FLOW

Ву

Walter Leo Maas

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EXPERIMENTAL DETERMINATION OF PITCHING MOMENT AND DAMPING COEFFICIENTS OF A CONE IN LOW DENSITY, HYPERSONIC FLOW

Ву

Walter Leo Maas

A portion of a Masters Thesis in Mechanical Engineering

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ABSTRACT

Values of the stability derivatives $C_{m_{\alpha}}$ and $C_{m_{q}}$ have been determined experimentally for cones with semi-vertex angles of 45° and 9°, and the results compared with theoretical estimates and with other experimental data. $C_{m_{\alpha}}$ is seen to be a function of angle of attack, and $C_{m_{\alpha}}$ is found to be positive, indicating negative damping. The influence of viscous effects upon these results is discussed.

The experiment was conducted with freely oscillating models in hypersonic, low density flow, and is one of the first dynamic stability tests performed under these flow conditions. $C_{m_{\alpha}}$ deviates sharply from linear theory, the non-linearity being even stronger than predicted by durrent non-linear Newtonian flow theory.

C_m was found to be positive in sign, meaning negative damping and an input of energy to the model from the flow. This instability is a marked deviation from the ordinary assumption of positive stability and certainly warrants further study and investigation. The cause of the instability remains undetermined; the effects of viscous flow and shedding of vortices is discussed in this connection.

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LIST OF SYMBOLS

(Other Symbols are defined as used)

b coefficient of damping term =
$$\frac{\rho USL^2}{2I}$$
 (- C_{m_q})

 C_m standard non-dimensionalized moment coefficient

 C_{m_Q} restoring moment derivative

 C_{m_q} damping derivative

 \overline{C}_{m_Q} : \overline{C}_{m_q} average values. See Section 5

D rate of decay of oscillation (°/sec)

I mass moment of inertia about axis of oscillation

k coefficient of restoring moment term = $\frac{\rho U^2 SL}{2I}$ (- C_{m_Q})

L reference length = axial length of cone

M Mach number

Re/in Reynolds number per inch = $\frac{u\rho}{v}$

S reference area = base area of cone

to axis of revolution, respectively

period of oscillation = $\frac{2\pi}{\omega}$

T

U velocity of undisturbed airflow

X distance from nose of cone to center of oscillation

α angle of attack

α oscillation angle or envelope of angle of attack

γ cone semi-vertex or half angle

ρ mass density of atmosphere

φ phase angle

θ angle of rotation

angular velocity or frequency

1. INTRODUCTION

The motion of an oscillating cone is described by the well-known second order differential equation containing inertia, damping and restoring moment terms. These terms can be evaluated experimentally by study of the motion in a wind tunnel airstream. This report covers such a test in low density, hypersonic flow; it is in the nature of a feasibility study since there is little background of dynamic stability tests under such conditions.

1.1 Theoretical Basis

The linearized equation of motion of natural short period longitudinal oscillations is given by Laitone as

$$I\dot{\theta} + \sqrt{\frac{\rho_{\text{USL}}}{2}} \frac{\partial c_{\text{m}}}{\partial \alpha} w + \sqrt{\frac{\rho_{\text{USL}}^2}{2}} \frac{\partial c_{\text{m}}}{\partial \left(\frac{\dot{\theta}_{\text{L}}}{u}\right)} \dot{\theta}$$

$$+ \sqrt{\frac{\rho_{\text{SL}}^2}{2}} \frac{\partial c_{\text{m}}}{\partial \left(\frac{\dot{\alpha}_{\text{L}}}{u}\right)} \dot{w} = 0$$
(1)

It can be shown that $\partial C_m/\partial \left(\frac{\dot{c}L}{u}\right)$ is negligible in hypersonic, low density flow, leaving

$$\begin{split} I\ddot{\theta} + \begin{pmatrix} \frac{\rho u S L}{2} & c_{m_{\alpha}} \end{pmatrix} w + \begin{pmatrix} \frac{\rho u S L^{2}}{2} & c_{m_{q}} \end{pmatrix} \dot{\theta} &= 0 \qquad (2) \\ \\ where & c_{m_{\alpha}} &= \frac{\partial c_{m}}{\partial \alpha} \\ \\ c_{m_{q}} &= \frac{\partial c_{m}}{\partial \left(\frac{\dot{\theta} L}{u}\right)} & \dot{\alpha} &= 0 \\ \\ \dot{\alpha} &= 0 \\ \dot{\alpha} &= 0 \\ \end{split}$$

This is an ordinary second order linear differential equation, with the linearization implying small values of θ .

1.2 Induced Oscillation Technique

It was first proposed (by Professor E. V. Laitone of the University of California) that the stability coefficients of a cone be evaluated by an induced oscillation technique in the wind tunnel. The cone model would be fixed on a shaft (sting) passing through and perpendicular to the axis of revolution of the cone. This sting would be mounted in bearings and the model, with sting, would be free to revolve in these bearings. However, the bearing supports, and therefore the model, would be oscillated in a plane perpendicular to the flow, with a velocity

$$\dot{z}(t) = a\omega \sin \omega t \tag{3}$$

where a = amplitude of oscillation
z = linear displacement of sting
ω = frequency of oscillation

Then in a wind tunnel of velocity U = u

$$\frac{\mathbf{w}}{\mathbf{U}} = \left(\theta + \frac{\dot{\mathbf{z}}}{\mathbf{U}}\right) = \theta + \frac{\mathbf{a}\omega}{\mathbf{U}} \sin \omega \mathbf{t} \tag{4}$$

and Equation (2) becomes

$$\theta + b\dot{\theta} + k\theta = -k \frac{a\omega}{U} \sin \omega t$$
 (5)

where
$$b = \frac{pUSL^2}{2I} \left(-C_{m_q}\right)$$

$$k = \frac{\rho U^2 SL}{2I} \left(-C_{m_{CY}} \right) \cdots$$

By measuring the amplitude $(\dot{\theta})$ and phase angle $(\phi_{\dot{\theta}})$ of the angular velocity $\dot{\theta}$ at different frequencies ω , C_{m} and C_{m} can be determined by a circle or Nyquist plot (see reference 2), where

vector length =
$$\frac{|\dot{\theta}|}{\omega a/L} = -\frac{C_{m_{\alpha}}}{C_{m_{q}}} \cos \phi_{\dot{\theta}} (\dot{\omega}) = \frac{|\dot{\theta}|}{a/L}$$

vector angle = $\phi_{\dot{\theta}} (\dot{\omega})$
= $\tan^{-1} \left[\frac{U}{\omega L} \frac{C_{m_{\alpha}}}{C_{m_{q}}} - 2 \frac{I/\rho SL^{3}}{\frac{U}{\omega L} \left(- C_{m_{q}} \right)} \right]$

$$= \phi_{\theta} (\dot{\omega}) + \frac{\pi}{2}$$
(6)

Therefore, in principle, the aerodynamic derivatives C_{m} and C_{α} can be found. However, it will be shown in Section 2.1 that this c_{q} method is not feasible in hypersonic flow, and it is necessary to turn elsewhere for an acceptable technique.

1.3 Free Oscillation Technique

In this method the model is free to oscillate in the sting bearings as before, however the bearings remain stationary. The motion of the model is purely oscillation about a fixed axis, under the influence of bearing friction and aerodynamic forces. Here

$$\theta = \frac{\mathbf{w}}{\mathbf{U}} = \alpha, \quad \frac{\dot{\mathbf{w}}}{\mathbf{U}} = \dot{\theta} = \dot{\alpha}, \quad \frac{\dot{\mathbf{w}}}{\mathbf{U}} = \dot{\theta} = \ddot{\alpha}$$
 (7)

and Equation (2) becomes

£.

$$\ddot{\alpha} + b\dot{\alpha} + k\alpha = 0 \tag{8}$$

Adding an arbitrary bearing friction torque f(G) gives the equation of motion of the system

$$\alpha + b\dot{\alpha} + f(\dot{\alpha}) + k\alpha = 0$$
 (9)

With small damping, the frequency of oscillation is

$$\omega = \sqrt{k} = \sqrt{\frac{\rho U^2}{2} \frac{SL}{I}} \quad (-C_{m_{Q}})$$
or $C_{m} = -\omega \frac{2}{\rho U^2} \frac{I}{SL} = -\left(\frac{2\pi}{T}\right)^2 \frac{2}{\rho U^2} \frac{I}{SL}$
(10)

The derivative C is a measure of the aerodynamic damping q present. This damping in turn can be found by observing the rate of decay of the oscillation amplitude as the model is given an initial displacement and allowed to oscillate in the flow stream.

2. PRELIMINARY CONSIDERATIONS

From the beginning of this program it was apparent that the aerodynamic damping would be small compared to the restoring moment.

Since

$$\frac{b}{k} = \frac{C_{m_q}}{C_{m_{q'}}} \frac{L}{U}$$
 (11)

and using estimated values

then $b/k = 10^{-4}/3$, an extremely small amount of damping. The factor L/U shows the difficulty; in hypersonic flow and with the model size restriction imposed by the flow nozzle, L/U becomes very small.

2.1 Induced Oscillation Technique

Equation (6) can be written

$$\varphi_{\theta}(\omega) = \tan^{-1} \frac{\frac{k}{\omega} - \omega}{b}$$

$$= \tan^{-1} \frac{\omega c^{2} - \omega^{2}}{\omega b}$$
(12)

where ω_0 = natural or undamped oscillatory frequency = \sqrt{k}

Since b is small, ω will be very close to ω_0 and any slight fluctuation in this difference will have a strong effect upon the vector position.

A preliminary calculation, using typical M=6 low density flow values and a 45° semi-vertex angle cone model with L=0.625 in,

showed that a frequency $\omega=1.0015~\omega_{o}$ would shift the phase vector to $\phi=45^{\circ}$, and $\omega=1.0060~\omega_{o}$ corresponds to $\phi=84.3^{\circ}$. Tunnel flow characteristics are such that ρU^{2} fluctuates as much as \pm 2%, and since $\omega_{o}\sim\sqrt{\rho U^{2}}$, ω_{o} would vary \pm 1%. Such a natural frequency variation would cause almost a 180° oscillation in the phase vector, rendering it useless in determining the aerodynamic coefficients and derivatives.

Essentially, the small amount of damping forces the induced frequency (ω) to be very close to the natural frequency (ω) in order to use the Nyquist plot, and with the flow irregularities inherent in the wind tunnel, ω_0 fluctuates enough to make $\phi = \tan^{-1} (\omega_0^2 - \omega^2)/\omega b$ completely undefinable. This conclusion resulted in abandonment of the induced oscillation technique.

2.2 Free Oscillation Technique

Determination of C_{m_Q} by observing the period of oscillation presented no serious problems, however the low aerodynamic damping again gave difficulty in finding C_{m} . The amplitude decay caused by bearing q friction would be relatively large and could easily obscure the aerodynamic damping. Information on low-friction bearings gave a minimum of 7 dyne-cm of resistance torque for the proposed system. Using this figure, calculations at M=6 flow conditions showed that the damping from the bearings would be approximately 10 times the aerodynamic damping.

On the basis of this information, it was decided to use the free Oscillation technique to determine C_{m} , with the possibility that C_{m} could also be found. C_{m} would be a function of the difference in decay rate between the model oscillating in the airflow and oscillating in the evacuated tunnel without flow. This relationship is described in detail in Appendix A.

3. EXPERIMENTAL EQUIPMENT

The tests were conducted in the No. 4 low density wind tunnel at the University of California Aeronautical Sciences Laboratory, Richmond Field Station. The Mach 6 nozzle was used, providing a test section approximately 2.5 inches in diameter. The fixture holding the model was mounted directly on the end of the nozzle, as shown in Figure 1.

Figure 2 shows the 9° cone model mounted on the fixture. The model is fixed on the vertical sting, the sting being supported by two electrically vibrated bearings. A cross shaft is mounted on the sting above the upper bearing. One arm of this shaft carries a blade which interrupts the light beam to a photocell as the model passes through zero angle of attack. The other arm is attracted by an electromagnet mounted on the tunnel, thereby pulling the model to an angle of attack. Release of the arm starts the oscillation. In addition, a shadow cast by this arm is projected upon a calibrated screen, providing direct oscillation angle (α_0) information.

As shown in Figure 1, a cardboard and plastic cover shields the arm from extraneous air currents. The quartz fiber is shown suspended from above and attaches to the tip of the sting. The sting itself (here carrying the 45° cone) has a tungsten carbide center section 2 inches long and 0.078 inches in diameter. This design represents a compromise between sting structural stiffness and minimum aerodynamic interference, several configurations were tried with this being the most satisfactory.

The photocell output is fed to an electronic counter which times the interval between pulses and presents this time on a visual readout. Since the swinging arm interrupts the photocell beam twice

complete oscillation, the time shown is one half the period of oscillation.

The bearings have an electrically vibrated inner bearing race, which reduces friction torque to a minimum by eliminating static friction. They are the most suitable bearings that could be found for this application, although devices such as air and magnetic suspension may have even less friction. These possibilities were not explored.

4. EXPERIMENTAL PROCEDURE AND DATA REDUCTION

The model was given an initial displacement of approximately 35° and allowed to oscillate in the flow stream. Oscillation period data from the electronic counter was recorded at $\alpha_{\rm o}$ = 30°, 20°, 15°, 10°, 5°, and 3°. This period gave $C_{\rm mi_{Cl}}(\alpha_{\rm o})$ directly through the relationship

$$C_{M_{\alpha}} = -\left(\frac{2\pi}{T}\right)^2 \frac{2I}{\rho U^2 SL}$$

As the motion decayed through values of $\alpha_0 = 30^\circ$, 20° , 15° , 10° , and 5° , the time was recorded. The average decay rate was computed in the intervals between these values by dividing the particular interval (in degrees) by the time the model took to decay through this interval. This value was taken as the decay rate at the angle in the mid-point of the interval. For example, in the interval between 15° and 10° , the decay

rate would be the interval (5°) divided by the decay time (in seconds) from 15° to 10°. This value is then the decay rate existing at α_0 = 12.5°.

As described in Appendix A, this decay test is performed under both no flow and flow conditions, the difference in rate of decay giving the value of C_{mq} . Using this method, C_{mq} can be found for $\alpha_0 = 25^{\circ}$, 17.5° , 12.5° , and 7.5° .

4.3 Other Parameters

The moment of inertia of the system (I) was computed as described in Appendix B. S and L were accurately measured using ordinary machine shop techniques. Flow information (O, M, U, and Re/in) were computed from compressible flow charts using flow pressure and temperature data recorded with each run.

5. RESULTS

Two cone models were tested, one having a semi-vertex angle $\gamma = 45^{\circ}$, and the other $\gamma = 9^{\circ}$. For the 45° cone, X/L = 0.337, for the 9° cone, X/L = 0.350. The average flow conditions in these tests were M = 6.05, Re/in = 11,700, U = 2375 ft/sec, $\frac{\rho U^2}{2} = 0.0530$ psi, and a static pressure of 125 microns of mercury.

Values of $C_{m_{\alpha}}$ are tabulated in Figure 3 and shown in graphical form in Figure 4. $C_{m_{q}}$ is plotted in Figure 7. These values are given as functions of C_{o} , the angle of oscillation. No attempt has been made to define them as functions of the instantaneous angle of attack, (α) , and since both $C_{m_{\alpha}}$ and $C_{m_{q}}$ vary with angle of attack, the figures given represent an average or effective value over a single

oscillation. Hereafter these effective values will be designated as $\overline{c}_{m_{\mathbf{q}}}$ and $\overline{c}_{m_{\mathbf{q}}}$.

EXPERIMENTAL ACCURACY

A numerical error analysis is given in Appendix C; the figures below are derived therein.

The uncertainty in the values of \overline{C}_{m_Q} is between 3.0% and 3.6%, depending upon α_o . The prime contributors to this inaccuracy are U, T, and α_o . The error in U is inherent in the flow stream and cannot be improved with the present tunnel and nozzle. The uncertainty in T is based upon data scatter; refinement of technique could possibly lower this somewhat. The inaccuracy in α_o is discussed fully in the next section. These values of \overline{C}_{m_Q} are about as precise as presently possible; it would be difficult to better them significantly without improving U.

6.2
$$\overline{\overline{c}}_{m_q}$$

The small magnitude of damping and the relatively crude decay rate measurements lead to the large uncertainties in \overline{c}_{m} . It is felt that a more sophisticated experimental system is necessary to derive accurate data.

The difficulties arise with the measurement of α_0 and with the bearing friction. The present method of reading α_0 (shadow of swinging arm projected on a calibrated screen) causes the 29% uncertainty in decay rate data; an improved system here would definitely improve the measured value of \overline{C}_m .

Aerodynamic damping is small compared to damping from bearing friction, consequently in the subtraction of decay rates (see Appendix A) two nearly equal numbers with moderate uncertainties are subtracted, the difference being small in magnitude and having a large uncertainty.

A solution here would be to reduce bearing friction. The bearings used are claimed to be the best conventional bearings available, however devices such as air suspension and suspension by fibers would warrant investigation for further experiments.

7. DISCUSSION OF RESULTS

7.1
$$\overline{c}_{m}$$

Figure 4 presents the experimentally derived values and compares them with other data, both theoretical and experimental.

On the ordinate $\alpha_{_{0}}=0$ the small angle values of $C_{_{_{1}}}$ from the theory of Coakley, Laitone, and Maas 3 and also from Tobak and Wehrend 4 are plotted. They are seen to be inreasonable agreement with the experimental values, the 45° cone particularly. Both theoretical analyses require $\alpha<\gamma$ (all elements of the cone must "see" or face the flow), the 9° cone is near this limit even at small $\alpha_{_{0}}$, which might explain the great deviation.

The bottom curve is from the experimental data of Maslach and Talbot⁵ (obtained under the same flow conditions as this report) on the static moment of a 9° cone. From their plot of $C_{\rm m}$ vs α (corrected for center of oscillation position) the slope of the secant line between $\alpha=0$ and $\alpha=\alpha_{\rm o}$ was taken as the average slope of $C_{\rm m}$ during an oscillation bounded by $\alpha_{\rm o}$. Therefore the values plotted are $\overline{C}_{\rm m}$ and

are directly comparable to the experimental values. It is seen that \overline{C}_{m} from the static test is generally smaller than that from the dynamic test and varies less with angle of attack. These differences are probably caused by unsteady flow effects around the oscillating cone and are seen to be appreciable in this hypersonic, low density flow regime.

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Charwat⁶ develops a Newtonian flow analysis for the normal force derivative $C_{N_{\alpha}}$ (which is proportional to $C_{m_{\alpha}}$ assuming a stationary center of pressure) for $\alpha < \gamma$ and also for the case where half of the surface of the body sees the flow. For a cone this latter solution is strictly valid for $\alpha = 90^{\circ}$ only, but the extension of this theory to lower angles of attack can give an indication of the variance of $C_{m_{\alpha}}$ with α (or α_{0}) for the 9° cone.

The two solutions of Charwat are shown in Figure 5, with a curve (dashed line) faired between the two being more representative of the actual case. It is seen that $C_{N_{\alpha}}$ (and therefore $C_{m_{\alpha}}$) generally increases with angle of attack up to α = 35°. This correlates well with the experimental values of $C_{m_{\alpha}}$ for the 9° cone shown in Figure 4, where $\overline{C}_{m_{\alpha}}$ is seen to increase with α_{o} .

Coakley, et. al., also give a hypersonic, Newtonian flow motion analysis not restricted to small angles of attack, requiring only that $\alpha < \gamma$. Their non-linear equation of motion is (disregarding damping):

$$\alpha + \frac{\rho U^2}{2I} SL \left[\frac{4}{3} - 2 \frac{X}{L} \cos^2 \gamma \right] \frac{\sin 2\alpha}{2} = 0$$
 (13)

Using the expansion $\frac{1}{2} \sin 2\alpha = \alpha - \frac{2}{3} \alpha^3 + \dots$ the frequency of oscillation of motions governed by this equation is

$$\omega = 2\pi \sqrt{\frac{\rho_U^2}{2} \frac{SL}{L} \left[\frac{4}{3} - 2 \frac{X}{L} \cos^2 \gamma \right]} \sqrt{1 - \frac{1}{2} \alpha_o^2}$$
 (14)

Figure 6 compares this relationship ρ , V, S, L and I taken the same as in experiment) with the frequencies obtained in the 45° cone experiment. It is seen that the decrease in ω with larger α_0 is even stronger than predicted by the non-linear theory.

Apparently, these differences are caused by viscous effects. Newtonian flow theory, of course, does not consider the boundary layer and wake phenomena which certainly influence the motion, especially at large α . Very little is known about hypersonic viscosity effects upon dynamic stability; the experimental results here indicate that they are appreciable and should be further investigated.

It should be noted that all the values of \overline{C}_m are negative, indicating positive static stability in equations (8) and (9). For the case of a missile returning to earth through the atmosphere, Allen shows that it is only necessary that $C_m < 0$ for static stability, after considering the effects of the earth's gravitational field, deceleration due to aerodynamic drag and variance of atmospheric density with the altitude. Thus, it seems that static stability of a conical missile is assured as long as the center of gravity (and therefore the axis of oscillation) is well forward, as in these tests. As Allen points out, however, static instability can occur with a c.g. position towards the rear of the missile.

It is felt that the values of $\overline{C}_{m_{\alpha}}$ found in these experiments are representative of the models tested. It is not possible to improve the experimental accuracy significantly without improving the flow

characteristics of the wind tunnel. However, it does seem that tests with the center of oscillation moved aft would be worthwhile, since a point would be reached where $C_{m_{\alpha}} > 0$ and the cone is statically unstable. For small α this point would be near the center of pressure, but for larger oscillations (as in these tests) the point of instability cannot be predicted theoretically, and a wind tunnel test is called for.

7.2
$$\overline{C}_{m}$$

The values of \overline{C}_{m_q} shown in Figure 7 have such a high experimental uncertainty that they must be considered in a qualitative sense only. Very little can be said of their absolute magnitude, except that perhaps \overline{C}_{m_q} for the 45° cone decreases with α_o and for the 9° cone increases with α_o .

It should be realized that \overline{C}_{m_q} has been found to be positive, indicating negative damping and dynamic instability. In every test on both cones, the model took longer to decay (from 30° to 5°) when under flow than it did with no flow. This is indicative of energy input into the model from the airflow.

This instability here only partially counteracts the bearing friction damping, and the oscillations still decrease. However, in an object in free flight, instability would tend to cause increasing oscillations (disregarding the influence of other damping factors, of course). For this reason it is apparent that the instability found here is important and should be investigated further.

All the available theory predicts $c_{m_{f q}} < 0$, and previous experiments (at lower Mach numbers) show $c_{m_{f q}} < 0$ and nearly independent

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of the angle of attack. It must be emphasized, though, that hypersonic Newtonian flow theory does not consider any variation in the pressures on the rear of a cone, and this effect could be important for a cone oscillating in a flow stream. An analytical study, one including viscous effects and not restricted to small α , would certainly be difficult, but might reveal the nature of this instability.

There seem to be no prior dynamic stability experiments of this type in hypersonic flow. Further investigation is certainly in order, both to more accurately determine $C_{m_{\widetilde{q}}}$, and especially to investigate the nature of the instability.

As stated earlier, the large uncertainty in \overline{C}_{m_q} stems from the small amount of damping present. With the model size restriction of the flow nozzle, the ratio b/k will be small in hypersonic flow unless \overline{C}_{m_q} (and therefore k) is reduced by oscillating the model on an axis near the center of pressure. Unfortunately, reducing the restoring moment in this manner increases the adverse effect of bearing friction, so this method most likely would not be an improvement.

Perhaps a free flight 'shot' in a ballistic-type tunnel would be the solution--here there would be no bearing friction and the model would oscillate about its center of mass. High speed photographs could provide an oscillation-time history; the decay (or increase) in the oscillation would give the damping. However, deceleration from aerodynamic drag introduces other terms into the damping coefficient; these might prove difficult to separate from \overline{C}_m .

More accurate determination of \overline{C}_m would be possible by improvement of the present apparatus. The uncertainty in α_0 (\pm 1°) is large and certainly could be decreased. An improved optical system or high speed motion pictures might be the solution.

Decreasing the bearing friction would increase the relative effect of the aerodynamic damping and thereby improve the accuracy of \overline{C}_m . The bearings used here are probably as friction free as possible in a mechanical system, but perhaps could be improved slightly. Magnetic or air suspension might be feasible, although it would be difficult to avoid the air or magnetic field affecting the motion of the model.

Suspension by a quartz fiber has definite possibilities, for quartz has very little internal friction and a quartz torsional pendulum decays very slowly. A model made from a heavy material such as lead could be hung in the airflow from a quartz fiber, perhaps with another fiber holding it from below.

Reducing the friction of the suspension device and decreasing the uncertainty in α_0 would permit an accurate plot of α_0 vs time. The slope of this curve could easily be found by use of a least squares program on a digital computer. This would eliminate the averaging method used in this report and provide accurate values of decay rate at any α_0 .

Another avenue for further investigation is the cause of the negative damping. As previously mentioned, there has been no prior indication of dynamic instability from either theoretical or experimental studies, although little work has been done in either field on oscillating bodies in hypersonic flow.

Possibly the instability is due to the asymmetrical shedding of vortices from the sharp trailing edge of the cone. Very little is understood about vortex formation on three-dimensional oscillating bodies, but it is possible to make a few statements concerning their effect.

It is known that vortices depart in a periodic manner from stationary bodies of revolution at zero angle of attack, and that they affect the pressure distribution on the surface of the body. It seems reasonable, then, that pressures on an oscillating body are also affected by vortex formation. If these pressure fluctuations occur in a manner so as to transfer energy from the flow to the model (i.e., the additional torque from the pressure fluctuation acts in the same direction as the rotational velocity, rather than being a torque opposing the velocity as in ordinary positive damping) there is negative damping. This might well be what is happening here.

The vibration of electric power lines in a crosswind is well-known; this is an example of aerodynamic instability from vortex formation on a two-dimensional body. Goldstein speaks of the oscillatory nature of vortex departure behind a flat circular disc and also of vortex instability behind a two-dimensional cylinder. Unfortunately, none of the information available specifically pertains to an oscillating, three-dimensional body.

As a feasibility study, this program was successful first in that the induced oscillation technique was shown to be impractical, and also that \overline{C}_m could be easily determined by the free oscillation technique. \overline{C}_m was found to a rather poor degree of uncertainty, but q improvement of the experimental apparatus could produce more accurate results.

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APPENDIK A

DETERMINATION OF C

The aerodynamic derivative C is a function of the decay rate of the oscillations in the flow. However, bearing friction also contributes to decay; this effect must also be evaluated. Two separate decay tests were made, the first in the evacuated tunnel with no flow but with a quartz fiber serving as a torsion spring. The second test was the same as above (quartz spring was retained) except that the model was exposed to the airflow.

The equations of motion for these systems are:

No Flow

$$\dot{\alpha} + d\dot{\alpha} + f\alpha = 0 \tag{A-1}$$

Flow

$$\ddot{\alpha}$$
 + $b\dot{\alpha}$ + $d\alpha$ + $k\alpha$ + $f\alpha$ = 0

(A-2)

= $\ddot{\alpha}$ + $(b+d)\dot{\alpha}$ + $(k+f)\alpha$ = 0

where: d = effective damping coefficient of bearings and quartz fiber

f = restoring moment coefficient
 of fiber

 δ = logarithmic decrement of oscillations

$$\delta \approx \frac{(\alpha_o)_n - (\alpha_o)_{n+1}}{(\alpha_o)_n}$$

and $\delta = \frac{T}{2}B$ where $B = \alpha$ coefficient in general

$$\delta = \frac{(\alpha_o)_n - (\alpha_o)_{n+1}}{(\alpha_o)_n} = \frac{T}{2} B$$

$$B = \frac{2}{(\alpha_o)_n} - \frac{(\alpha_o)_n - (\alpha_o)_{n+1}}{T} = \frac{2}{(\alpha_o)_n} D$$

$$B_F = \frac{2}{(\alpha_o)_n} D_F = b + d$$

$$B_{NF} = \frac{2}{(\alpha_o)_n} D_{NF} = d$$

where the subscripts F and NF refer to the flow and no flow cases respectively

at any $\alpha_{_{\rm O}}$ can be found by measuring the decay rates under flow and no flow conditions. This analysis assumes that bearing friction produces linear (viscous) damping. The bearing friction is most likely nearer sliding or Coulomb friction, but here this non-linearity is neglected and has been replaced by the "equivalent" viscous damping.

VESENDIN B

MOMENT OF INERTIA DETERMINATION

The mass moment of inertia (I) was found by oscillating the system in an evacuated tunnel using the quartz torsion spring and observing the period of oscillation on the counter. Two tests were made, one with the system as used in the flow tests, and a second using an additional cross arm, of known moment of inertia I', attached to the sting. Since

$$T \sim I^{1/2}$$

then

$$\frac{T_{\text{with arm}}}{T_{\text{without arm}}} = \sqrt{\frac{I_{\text{w/arm}}}{I_{\text{w/o arm}}}}$$

or

$$I_{w/o \text{ arm}} = I = I_{w/a \text{rm}} \left(\frac{T_{w/o \text{ arm}}}{T_{w/a \text{rm}}}\right)^{2}$$

$$= (I' + I) \left(\frac{T_{w/o \text{ arm}}}{T_{w/a \text{rm}}}\right)^{2}$$

$$I = \frac{I' \left(\frac{T_{w/o \text{ arm}}}{T_{w/a \text{rm}}}\right)^{2}}{I \left(\frac{T_{w/o \text{ arm}}}{T_{w/a \text{rm}}}\right)^{2}}$$
(B-1)

This indirect method permits accurate determination of I without knowing the spring constant of the quartz spring. This test was performed with both the 9° and 45° cones, and in both cases $I' \approx 3I$.

APPENDIX C

ERROR ANALYSIS

 $\frac{\overline{c}_{m_{\alpha}}}{}$

The following undertainty values have been assigned:

$$\left(\frac{1}{2}\rho U^{2}\right)^{*} = \pm 2.0\%$$

$$I^{*} = \pm 0.4\%$$

$$S^{*}, L^{*} = \pm 0.2\%$$

$$U^{*} = \pm 1.0\%$$

$$T^{*} = 1.0\%$$

$$\alpha_{o}^{*} = \pm 1\%$$
where $\left(\frac{1}{2}\rho U^{2}\right)^{*}$, I^{*} , indicate uncertainty in I , etc.

A least count analysis would indicate an uncertainty of \pm 0.8% in $\left(\frac{1}{2}\rho U^2\right)^*$; however, past experience has shown that the figure of \pm 2% is more realistic due to non-uniform flow in the nozzle.

Using the 4-m-s method of error calculation,

$$C_{m_{\alpha}}^{*} = \pm \sqrt{(2T^{*})^{2} + (T^{*})^{2} + (T^{*})^{2} + (T^{*})^{2} + (T^{*})^{2}}$$

$$= \pm 2.9\%$$

This is the error in $C_{m_{\alpha}}$ as observed. Since there is an uncertainty in the value of α_{o} , an additional uncertainty in $C_{m_{\alpha}}(\alpha_{o})$ arises. Examples for both models will be given.

45° Cone

$$^{\mathrm{C}}_{\mathrm{m}_{\mathrm{C}}}$$
 changes about 0.009 per degree of $^{\mathrm{C}}_{\mathrm{O}}$

$$\alpha_{o} = 30^{\circ}$$

$$\frac{0.009}{0.765} = 1.2\%$$

$$\frac{0.009}{0.765} = 1.2\% \qquad c_{m_{CY}}^{*} = \sqrt{2.9^2 + 1.2^2} = 3.1\%$$

$$\alpha_0 = 15^{\circ}$$

$$\frac{0.009}{0.896} = 1.0\%$$

$$\frac{0.009}{0.896} = 1.0\%$$
 $C_{m_{\alpha}}^{*} = \sqrt{2.9^2 + 1.0^2} = 3.0\%$

9° Cone

$$c_{m}$$
 changes 0.008 per degree of α_{o}

$$\alpha_0 = 20^{\circ}$$

$$\frac{0.008}{0.761} = 1.1\%$$

$$\frac{0.008}{0.761} = 1.1\%$$
 $C_{m}^{*} = \sqrt{2.9^2 + 1.1^2} = 3.1\%$

$$\alpha_{\rm o} = 10^{\circ}$$
 (The worst case) - $C_{\rm m}$ changes 0.014 per degree of $\alpha_{\rm o}$

$$\frac{0.014}{0.666} = 2.1\%$$

$$\frac{0.014}{0.666} = 2.1\% \qquad c_{m_{CY}}^* = \sqrt{2.9^2 + 2.1^2} = 3.6\%$$

c_ma

The uncertainty for the 45° cone at $\alpha_0 = 12.5$ ° will be taken for illustration.

$$= \frac{(\alpha_0)_1 - (\alpha_0)_2}{t_2 - t_1} \qquad \frac{15^{\circ} - 10^{\circ}}{t_{10} - t_{15}}$$

The scatter of data indicates that the average time figures are accurate within \pm 2% , and using α_0^* = \pm 1°

$$\begin{cases} (\alpha_{0})_{1} - (\alpha_{0})_{2} = 15 - 10 = 5^{\circ} \\ \left[(\alpha_{0})_{1} - (\alpha_{0})_{2} \right]^{*} = \sqrt{1^{2} + 1^{2}} = 1.4 = 28\% \end{cases}$$

$$\begin{cases} t_{2} - t_{1} = 160 - 107 = 53 \quad \text{Flow Test} \\ \left[t_{2} - t_{1} \right]^{*} = \sqrt{3.2^{2} + 2.2^{2}} = 3.2 = 7.1\% \end{cases}$$

$$\begin{cases} t_{2} - t_{1} = 157 - 109 = 48 \quad \text{No Flow Test} \\ t_{2} - t_{1} = \sqrt{3.1^{2} + 2.2^{2}} = 3.8 = 8.0\% \end{cases}$$

$$D^{*} = \sqrt{\left[(\alpha_{0})_{1} - (\alpha_{0})_{2} \right]^{*2} + \left[t_{2} - t_{1} \right]^{*2}}$$

$$D^{*}_{F} = \sqrt{28^{2} + 7.1^{2}} = 29\%$$

$$D^{*}_{NF} = \sqrt{28^{2} + 810^{2}} = 29\%$$

$$D^{*}_{F} - D_{NF} = 0.09434 - 0.1042 = -0.0099$$

$$\begin{bmatrix} D_{F} - D_{NF} \end{bmatrix}^{*} = \sqrt{0.027^{2} + 0.030^{2}} = 0.041 = 410\% \end{cases}$$

 \overline{C}_{m} is a direct function of $D_{\overline{F}}$ - D_{NF} and therefore \overline{C}_{m} will have

an uncertainty of at least 410%. All other values of \bar{c}_{mq} show a similarly large uncertainty, this example being typical.

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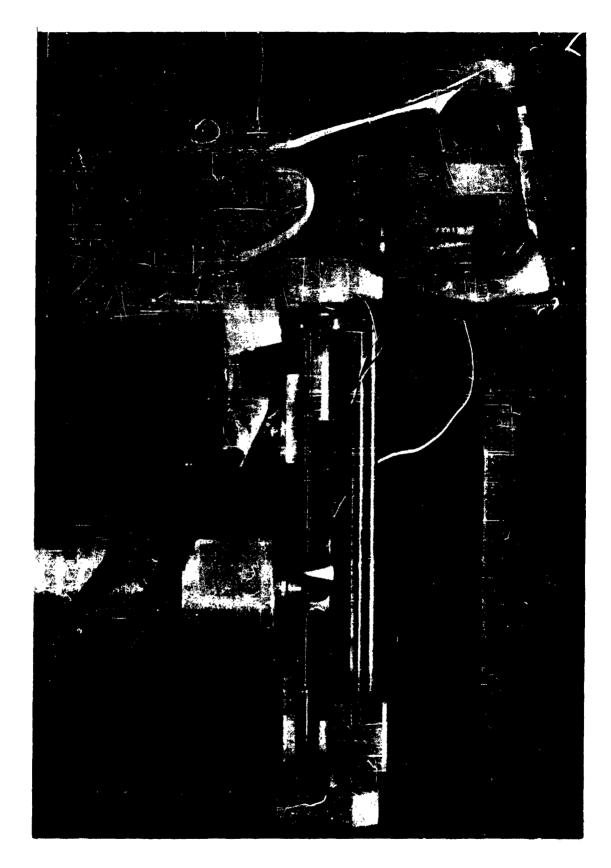


FIG. I FIXTURE MOUNTED ON NOZZLE WITH 45° CONE

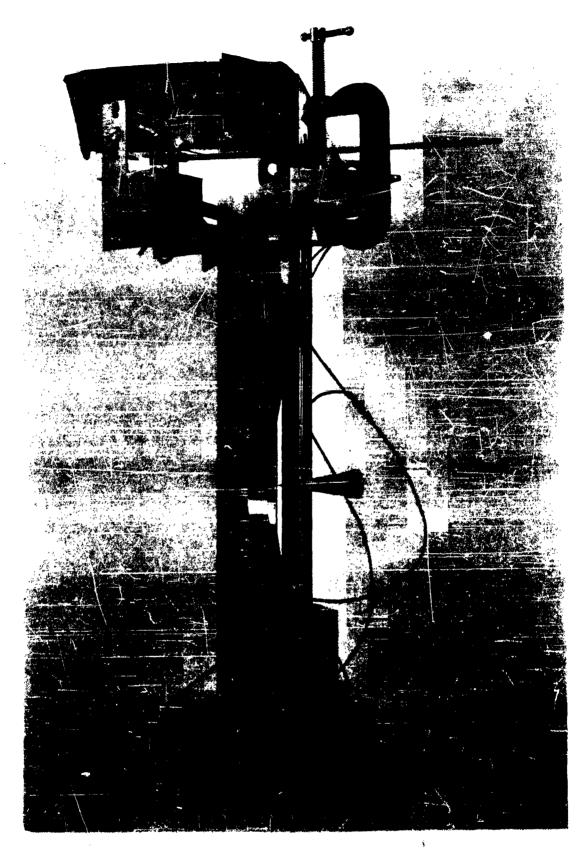
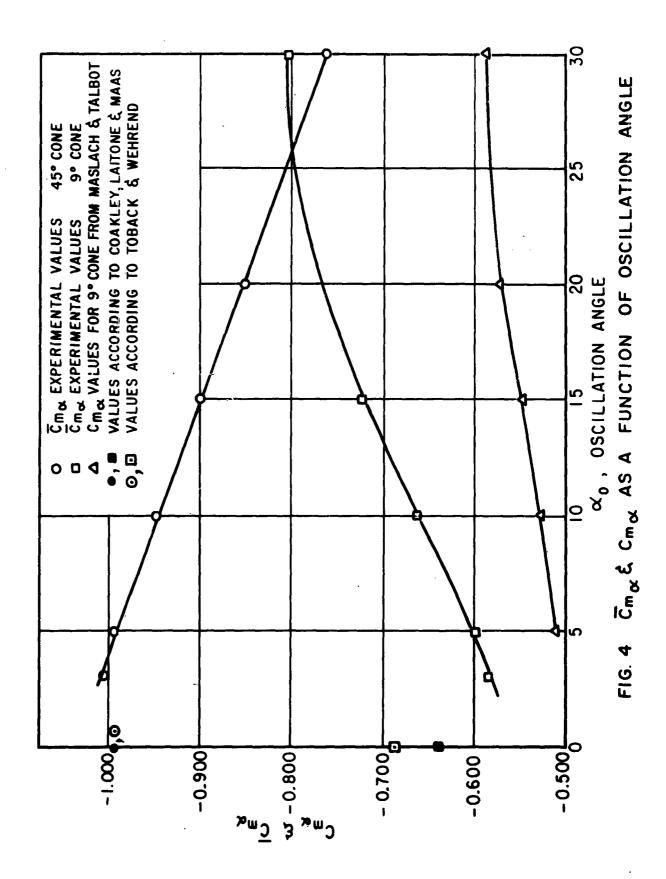
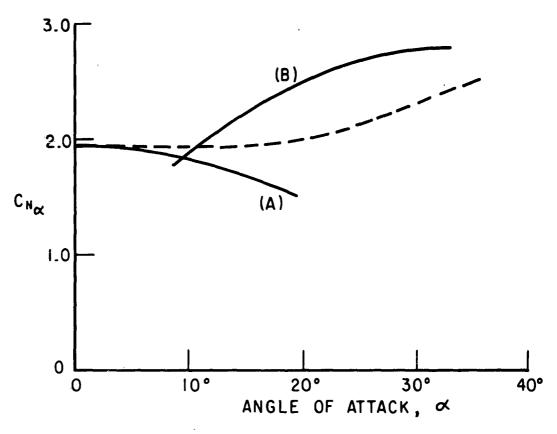


FIG. 2 FIXTURE WITH 9° CONE

α ₀	C _m 45°CONE	C _m ⊲ 9° CONE
3°	1.007	0.582
5°	0.994	0.598
10°	0.949	0.666
15°	0.896	0.722
20°	0.851	0.762
30°	0.765	0.803

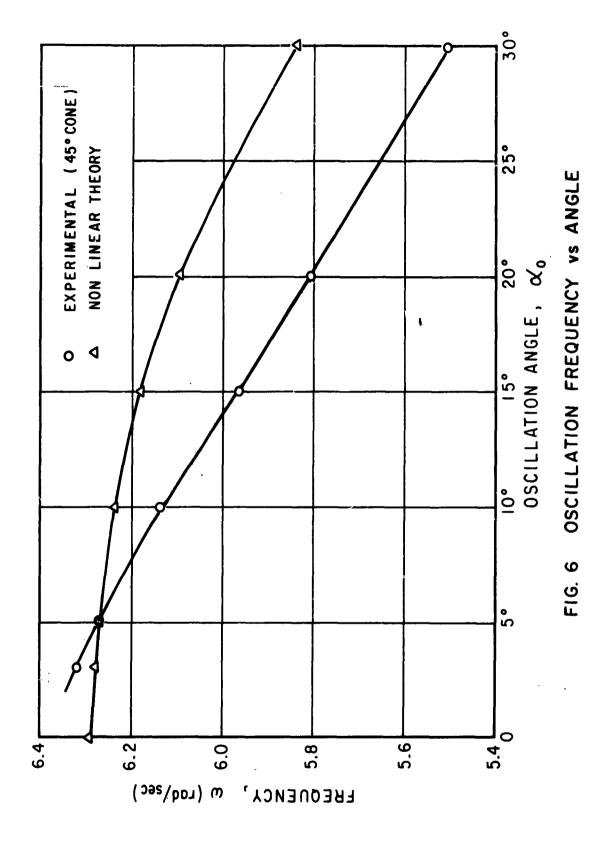
FIG. 3 VALUES OF $\overline{C}_{m_{\infty}}$ FOR VARIOUS OSCILLATION ANGLES (α_{o}). 45° ξ 9° SEMI- VERTEX ANGLE CONES.





- (A) SOLUTIONS FOR $\alpha < \delta$
- (B) SOLUTIONS FOR ONE HALF OF THE SURFACE SEEING THE FLOW.

FIG. 5 $C_{N_{\infty}}$ vs ∞ NEWTONIAN FLOW SOLUTION



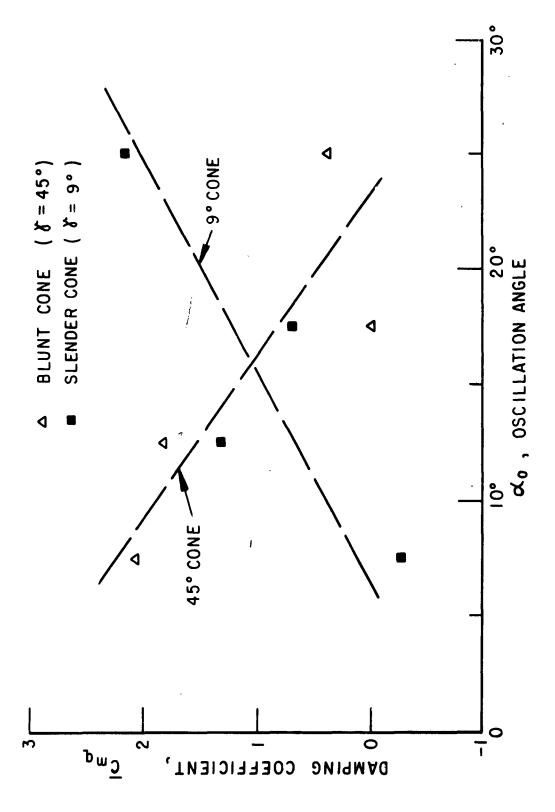


FIG. 7 PLOT OF Emq vs OSCILLATION ANGLE

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